	Prepared by: Asim Khan - 9/22/2012			
Timeline	Themes/Enduring Understandings/Essential Questions for the Unit	Common Core Standards	Standards Based Skills and Concepts Targeted	Assessments
		U	nit I Exploring Data: describing patterns and departures from patterns	
	How to construct and interpret graphical displays of distributions of univariate data?			To be assessed: The students will be assessed on mathematical and statistical accuracy, the
	Center and spread	HSS-ID.A.1	• CONSTRUCT and INTERPRET dotplots, stemplots, and histograms	students' conceptual understanding and their ability to communicate using the terminology of statistics.
1st Year - September	Clusters and gaps	HSS-ID.A.3	DESCRIBE the shape of a distribution	Collection
(Weeks 1 through 3)	Outliers and other unusual features	HSS-IC.B.6	USE histograms wisely	of evidence: • Quizzes will be given every other week • Homework, Classwork • Tests will be given every other week
	• Shape			• Notebook-A notebook will be kept that includes lesson notes, examples, student work, and corrections.
				Types of assessment:
				Academic prompt     Questions and Answer
	How to summarize distributions of univariate data?			Constructed response     Observation     Work Sample
	Measuring center: median, mean	HSS-ID.A.1	MEASURE center with the mean and median	Assessment Values: 15% Quizzes
	Measuring spread: range, interquartile range, standard deviation	HSS-ID.A.2	MEASURE spread with standard deviation and interquartile range	50% Tests 20% Classwork and Homework 15% Project
	Measuring position: quartiles, percentiles, standardized scores (z-scores)	HSS-ID.A.3	IDENTIFY outliers	Criteria by which the student responses will be evaluated:
1st Year -	Using boxplots	HSS-IC.B.6	CONSTRUCT a boxplot using the five-number summary	<ul> <li>Homework will be graded in class each day by stating answers out loud, placing work on the</li> </ul>
September (Week 4) and October (Weeks 1 through	• The effect of changing units on summary measures		CALCULATE numerical summaries with technology	board, or peer reviewing in cooperative learning groups • Homework quizzes will be graded on
2)			MEASURE position using percentiles	mathematical reasoning, accuracy, and presentation of work.
			INTERPRET cumulative relative frequency graphs	<ul> <li>Onit test will be graded on mathematical reasoning, accuracy, and presentation of work.</li> <li>Notes will be checked periodically for</li> </ul>
			MEASURE position using z-scores	completion and accuracy.
			TRANSFORM data	
			DEFINE and DESCRIBE density curves	
	How to compare distributions of univariate data?			
	Comparing center and spread: within group, between group variation	HSS-ID.A.1	COMPARE distributions	

## Strategies/Practices Used to Teach Skills and Concepts

# **Resources/Texts Used**

	Performance Tasks:	AP Statistics Text Book
	Collected homework and class work	College Board Resources
	Class Review	AP Practice
	Chapter Quiz	Standardized Test Preparation
	Chapter Test	· · · · · · · · · · · · · · · · · · ·
	<b>^</b>	
	Other evidence:	
	Daily observations – class problems	
	Daily homework checks	
	AP Practice	
	Student Self-Assessment/Reflection:	
	Independent class problems	
	Homework	
	Final Exams and review sheets	
1		
1		

1st Year - October (Weeks 3 and 4) and	Comparing clusters and gaps	HSS-ID.A.2	
November(Week 1)	Comparing outliers and other unusual features	HSS-ID.A.3	
	Comparing shape		
	How to explore bivariate data?		
	Analyzing patterns in scatterplots	HSS-ID.B.6	IDENTIFY explanatory and response variables
	Correlation and linearity	HSS-ID.B.6a	CONSTRUCT scatterplots to display relationships
	Least-squares regression line	HSS-ID.B.6b	INTERPRET scatterplots
	Residual plots, outliers, and influential points	HSS-ID.B.6c	MEASURE linear association using correlation
	Transformations to achieve linearity: Logarithmic and Power Transformations	HSS-ID.C.7	INTERPRET correlation
		HSS-ID.C.8	INTERPRET a regression line
1st Year - November (Weeks 2 through			CALCULATE the equation of the least-squares regression line
4) and December (Weeks 1 through 2)			CALCULATE residuals
			CONSTRUCT and INTERPRET residual plots
			DETERMINE how well a line fits observed data
			INTERPRET computer regression output
			USE transformations involving powers and roots to achieve linearity for a relationship between two variables
			MAKE predictions from a least-squares regression line involving transformed data
			• USE transformations involving logarithms to achieve linearity for a relationship between two variables
			• DETERMINE which of several transformations does a better job of producing a linear relationship
	How to explore categorical data?		
	Frequency tables and bar charts	HSS-ID.B.5	CONSTRUCT and INTERPRET bar graphs and pie charts



	Marginal and joint frequencies for two-way tables	HSS-CP.A.1	RECOGNIZE "good" and "bad" graphs	
	Conditional relative frequencies and association	HSS-CP.A.2	CONSTRUCT and INTERPRET two-way tables	
	Comparing distributions using bar charts	HSS-CP.A.3	DESCRIBE relationships between two categorical variables	
1st Year - January (Weeks 1 through 4)		HSS-CP.A.4	ORGANIZE statistical problems	
		HSS-CP.A.5		
		HSS-CP.B.6		
		HSS-CP.B.7		
		HSS-CP.B.8(+)		
		HSS-MD.B.7(+)		



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Timeline	Themes/Enduring Understandings/Essential Questions for the Unit	Common Core Standards	Standards Based Skills and Concepts Targeted	Assessments	Strategies/Practices Used to Teach Skills and Concepts	Resources/Texts Used			
	Unit II Sampling and Experimentation: planning and conducting a study								
	What are the methods of data collection?			To be assessed: The students will be assessed on	Performance Tasks: Collected homework and class work Class Review	AP Statistics Text Book     College Board Resources     AP Practice			
	• Census	HSS-ID.C.9	DESCRIBE the language of experiments	mathematical and statistical accuracy, the students' conceptual understanding and their ability to communicate using the	Chapter Quiz Chapter Test	Standardized Test Preparation			
Ist Year - February (Weeks	Sample survey	HSS-IC.B.3	IDENTIFY the population and sample in a sample survey	terminology of statistics. Collection	Other evidence: Daily observations – class problems Daily homework checks				
1 and 2)	Experiment	HSS-IC.B.5	IDENTIFY voluntary response samples and convenience samples	of evidence: • Quizzes will be given every other week • Homework, Classwork	AP Practice Student Self-Assessment/Reflection:				
	Observational study		DISTINGUISH observational studies from experiments	<ul> <li>Tests will be given every other week</li> <li>Notebook-A notebook will be kept that includes lesson notes, examples,</li> </ul>	Independent class problems Homework Final Exams and review sheets				
				student work, and corrections. Types					
				Selected response     Academic prompt					
				Questions and Answer     Constructed response					
	How to plan and conduct surveys?			Observation     Work Sample					
	Characteristics of a well-designed and well-conducted survey	HSS-IC.B.3	DESCRIBE how to use a table of random digits to select a simple random sample (SRS)	Assessment Values: 15% Quizzes					
lst Year - February (Weeks	Populations, samples, and random selection		DESCRIBE simple random samples, stratified random samples, and cluster samples	50% Tests 20% Classwork and Homework 15% Project					
3 and 4)	Sources of bias in sampling and surveys		EXPLAIN how undercoverage, nonresponse, and question wording can lead to bias in a sample survey	Criteria by which the student responses will be evaluated:					
	Sampling methods, including simple random sampling, stratified random sampling, and			<ul> <li>Homework will be graded in class each day by stating answers out loud, placing</li> </ul>					
	ciuster sampting			work on the board, or peer reviewing in cooperative					
				Homework quizzes will be graded on mathematical parconing, accuracy, and					
				presentation of work.					
	How to plan and conduct experiments?			<ul> <li>Unit test will be graded on mathematical reasoning, accuracy, and presentation of work.</li> </ul>					
	Characteristics of a well-designed and well-conducted experiment	HSS-ID.C.9	APPLY the three principles of experimental design	<ul> <li>Notes will be checked periodically for completion and accuracy.</li> </ul>					
lst Year - March	Treatments, control groups, experimental units, random assignments, and replication	HSS-IC.B.3	DESIGN comparative experiments utilizing completely randomized designs and randomized block designs, including matched pairs design						
(Weeks I and 2)	Sources of bias and confounding, including placebo effect and blinding	HSS-IC.B.5							
	Completely randomized designs								
	Randomized block design, including matched pairs design								
	What results and types of conclusions can be drawn from observational studies,			1					
	experiments, and surveys;								
		HSS-ID.C.9	DESCRIBE the challenges of establishing causation						
1st Year - March (Week 3)		HSS-IC.B.3	DEFINE the scope of inference						
			DESCRIBE data ethics in designing studies						

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		Unit III Ant	icinating Patterns: exploring random phenomena using probability and si	mulation	Concepts	
	What is anohability and have is it used?	Unit III An	actpacing 1 atterns, exploring random phenomena using probability and si	To be assessed:	Performance Tasks: Collected homework and class work	AP Statistics Text Book     College Board Resources
	<ul> <li>Interpreting probability, including long-run relative frequency interpretation</li> </ul>	HSS-ID.B.5	DESCRIBE the idea of probability	The students will be assessed on mathematical and statistical accuracy, the students' conceptual understanding and their ability to communicate using the	Class Review Chapter Quiz Chapter Test	AP Practice     Standardized Test Preparation
	Addition rule, multiplication rule, conditional probability, and independence	HSS-IC.A.2	DESCRIBE myths about randomness	terminology of statistics.	Other evidence: Daily observations – class problems Daily homework checks	
	Discrete random variables and their probability distributions, including binomial and     geometric	HSS-CP.A.1	DESIGN and PERFORM simulations	Quizzes will be given every other week     Homework, Classwork	Student Self-Assessment/Reflection:	
	Simulation of random behavior and probability distributions     mean (expected value) and standard deviation of a random variable, and micat	HSS-CP.A.2	DESCRIBE chance behavior with a probability model	Tests will be given every other week     Notebook-A notebook will be kept that     includes lesson notes, examples,	Independent class problems Homework Final Exams and review sheets	
	transformation of a random variable	HSS-CP.A.3	DEFINE and APPLY basic rules of probability	student work, and corrections. Types of assessment: • Selected response		
		HSS-CP.A.4	DETERMINE probabilities from two-way tables	Academic prompt     Questions and Answer     Constructed response		
		HSS-CP.A.5	CONSTRUCT Venn diagrams and DETERMINE probabilities	Observation     Work Sample     Assessment		
1st Year - March (Week 4) and		HSS-CP.B.6	DEFINE conditional probability     COMPLIE conditional probabilities	Values: 15% Quizzes 50% Tests 20% Classwork and Homework		
April (Weeks 1 through 3)		HSS-CP B 8(+)	CONFORCEMENTATION POWERTING     DESCRIBE chance behavior with a tree distram	15% Project Criteria by which the student responses will be		
		HSS-MD.A.1(+)	DEFINE independent events	evaluated: • Homework will be graded in class each day by stating answers out loud, placing		
		HSS-MD A 2(+)	DETERMINE whether two events are independent	work on the board, or peer reviewing in cooperative learning groups		
		HSS-MD.A.3(+)	APPLY the general multiplication rule to solve probability questions	<ul> <li>Homework quizzes will be graded on mathematical reasoning, accuracy, and presentation of</li> </ul>		
		HSS-MD.A.4(+)	APPLY the concept of discrete random variables to a variety of statistical settings	work. • Unit test will be graded on mathematical reasoning, accuracy, and presentation of		
		HSS-MD.B.5(+)	CALCULATE and INTERPRET the mean (expected value) of a discrete random variable	work. • Notes will be checked periodically for completion and accuracy.		
		HSS-MD.B.6(+)	CALCULATE and INTERPRET the standard deviation (and variance) of a discrete random variable			
		HSS-MD.B.7(+)	DESCRIBE continuous random variables			
			DESCRIBE the effect of performing a linear transformation on a random variable			
	How to combine independent random variables?					
	Notion of independence versus dependence	None	COMBINE random variables and CALCULATE the resulting mean and standard deviation			
1st Year - April (Week 4) and May (Weeks 1	Mean and standard deviation for sums and differences of independent random variables		CALCULATE and INTERPRET probabilities involving combinations of Normal random variables			
through 3) and 2nd Year - September						
(Weeks 1 through4)						
	What is the Normal distribution and how is it used?					
	Properties of the Normal distribution	HSS-ID.A.4	DESCRIBE and APPLY the 68-95-99.7 Rule			
1st Year - September (Week	Using tables of the Normal distribution		DESCRIBE the standard Normal Distribution			
(Weeks 1 through 2)	The Normal distribution as a model for measurements		PERFORM Normal distribution calculations			
			ASSESS Normality			
	What are sampling distributions and how are they used?					
	Sampling distribution of a sample proportion	HSS-IC.A.2	FIND the mean and standard deviation of the sampling distribution of a sample proportion			
	Sampling distribution of a sample mean	HSS-IC.B.5	• DELERMINE: whether or not it is appropriate to use the Normal approximation to calculate probabilities involving the sample proportion			
	Central Limit Theorem		CALCULATE probabilities involving the sample proportion			
	Sampling distribution of a difference between two independent sample proportions		<ul> <li>EVALUATE a claim about a population proportion using the sampling distribution of the sample proportion</li> <li>FIND the mean and standard deviation of the sampling distribution of a sample mean</li> </ul>			
	Sampling distribution of a difference between two independent sample means		CALCULATE probabilities involving a sample mean when the population distribution is Normal			
	Simulation of sampling distributions		EXPLAIN how the shape of the sampling distribution of sample means is related to the shape of the			
	Chisemen distribution		population distribution			
	- Cin-square unsurounoff		DISTINGUISH between a parameter and a statistic			
			DEFINE sampling distribution			
			DISTINGUISH between population distribution, sampling distribution, and the distribution of sample data			
2nd Year - October (Weeks 1 through 4) and			<ul> <li>DETERMINE whether a statistic is an unbiased estimator of a population parameter</li> </ul>			
November (Week 1 through 4)			DESCRIBE the relationship between sample size and the variability of an estimator			
			DETERMINE whether the conditions for performing inference are met.			

	INTERPRET the results of inference procedures in a randomized experiment.		
	DESCRIBE the characteristics of the sampling distribution of the difference between two sample means		
	CALCULATE probabilities using the sampling distribution of the difference between two sample means		
	DETERMINE whether the conditions for performing inference are met		
	USE two-sample t procedures to compare two means based on summary statistics or raw data		
	INTERPRET computer output for two-sample t procedures		
	PERFORM a significance test to compare two means		
	INTERPRET the results of inference procedures		
	COMPUTE expected counts, conditional distributions, and contributions to the chi-square statistic		
	CHECK the Random, Large sample size, and Independent conditions before performing a chi-square test		

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Timeline	Themes/Enduring Understandings/Essential Questions for the Unit	Common Core Standards	Standards Based Skills and Concepts Targeted	Assessments	Strategies/Practices Used to Teach Skills and Concepts	Resources/Texts Used
		Unit IV	Statistical Inference: estimating population parameters and testing hypo	thesis		
_		0	Survival interencer estimating population parameters and testing hypo	To be assessed:	Performance Tasks:	AP Statistics Text Book
	What is estimation (point estimators and confidence intervals) and how is it found?				Collected homework and class work	College Board Resources
				The students will be assessed on mathematical and statistical accuracy, the	Class Review Chapter Ouiz	AP Practice     Standardized Test Preparation
	<ul> <li>Estimating population parameters and margins of error</li> </ul>	HSS-IC.A.1	<ul> <li>INTERPRET a confidence level</li> </ul>	students' conceptual understanding and	Chapter Test	
				their ability to communicate using the terminology of statistics	Other evidence:	
	· Properties of point estimators, including unbiasedness and variability	HSS-IC.B.4	<ul> <li>INTERPRET a confidence interval in context</li> </ul>	commonly of subsect	Daily observations - class problems	
	· Logic of confidence intervals, meaning of confidence level and confidence intervals, and			Collection	Daily homework checks	
	properties of confidence intervals	HSS-IC.B.5	DESCRIBE how a confidence interval gives a range of plausible values for the parameter	Quizzes will be given every other week	Arriance	
2nd Year -				Homework, Classwork	Student Self-Assessment/Reflection:	
December (Weeks	<ul> <li>Large-sample confidence interval for a proportion</li> </ul>		<ul> <li>DESCRIBE the inference conditions necessary to construct confidence intervals</li> </ul>	<ul> <li>Tests will be given every other week</li> <li>Notebook-A notebook will be kept that</li> </ul>	Homework	
January (Weeks				includes lesson notes, examples,	Final Exams and review sheets	
1 through 4) and	· Large-sample confidence interval for a difference between two proportions		· EXPLAIN practical issues that can affect the interpretation of a confidence interval	student work, and corrections. Types		
1 and 2)				of assessment:		
	Confidence interval for a mean		<ul> <li>CONSTRUCT and INTERPRET a confidence interval for a population proportion</li> </ul>	Selected response     Academic prompt		
				Questions and Answer		
	Confidence interval for a difference between two means (unpaired and paired)		DETERMINE the sample size required to obtain a level C confidence interval for a population proportion     with a specified margin of error	Constructed response     Observation		
				Work Sample		
	Confidence interval for the close of a least-counter respection line		DESCRIBE how the margin of error of a confidence interval changes with the sample size and the level of	Assessment Values:		
	confidence interval for the stope of a reast-squares regression line		confidence C	15% Quizzes		
			• DED COD M a similar test to summer two momentum	50% Tests 20% Classwork and Homework		
			<ul> <li>FERTORM a significance test to compare two proportions.</li> </ul>	15% Project		
				Criteria		
				evaluated:		
				<ul> <li>Homework will be graded in class each durcher station and sharing</li> </ul>		
	what are the types of tests of significance and now are they usea?			work on the		
	<ul> <li>Logic of significance testing, null and alternative hypothesis; P-values; one-and two-sided tests; concepts of Type I and Type II errors; concept of power</li> </ul>			board, or peer reviewing in cooperative		
		HSS-IC.A.I	<ul> <li>CONSTRUCT and INTERPRET a confidence interval to compare two proportions.</li> </ul>	<ul> <li>Homework quizzes will be graded on</li> </ul>		
				mathematical reasoning, accuracy, and		
	<ul> <li>Large-sample test for a proportion</li> </ul>	HSS-IC.A.2	<ul> <li>STATE correct hypotheses for a significance test about a population proportion or mean.</li> </ul>	work.		
	the state the state of the	USE ICE 4	DITTIONIT D. L. S. L.	Unit test will be graded on mathematical		
	Large-sample test for a difference between two proportions	HSS-R.,B.4	INTERPRET P-values in context.	work.		
				<ul> <li>Notes will be checked periodically for</li> </ul>		
	Iest for a mean	HSS-IC.B.5	<ul> <li>INTERPRET a Type I error and a Type II error in context, and give the consequences of each.</li> </ul>	completion and accuracy.		
	<ul> <li>Test for a diffence between two means (unpaired and paired)</li> </ul>		DESCRIBE: the relationship between the significance level of a test, P(Type II error), and power			
	· Chi-square test for goodness of fit, homogeneity of proportions, and independence (one-					
	and two-way tables)		<ul> <li>CHECK conditions for carrying out a test about a population proportion.</li> </ul>			
	<ul> <li>Test for the slope of a least-squares regression line</li> </ul>		<ul> <li>CONDUCT a significance test about a population proportion.</li> </ul>			
			· CONSTRUCT a confidence interval to draw a conclusion about for a two-sided test about a population			
2nd Year -			proportion.			
February (Weeks 3 and 4) and						
March (Weeks 1			<ul> <li>CHECK conditions for carrying out a test about a population mean.</li> </ul>			
April (Week 1)						
			<ul> <li>CONDUCT a one-sample t test about a population mean.</li> </ul>			
			concentration of the lands of the second states and the second states and the			
			<ul> <li>CONSTRUCT a confidence interval to draw a conclusion for a two-sided test about a population mean.</li> </ul>			
			PEPEOPM similicance tests for mixed data			
			· race of a significance cost for pareed data.			
			· PERFORM a chi-square goodness-of-fit test to determine whether sample data are consistent with a			
			specified distribution of a categorical variable			
			• EXAMINE individual commonents of the chi-source statistic as part of a full-source scalario			
			a control of a follow-up analysis			
			• CHECK and iting for a family information hout the stars 0 of the part of			
			<ul> <li>CELCER conditions for performing inference about the stope p of the population regression line</li> </ul>			
			CONSTRUCT and INTERDRET - and dama into the data to the data to			
			<ul> <li>CONSTRUCT and INTERPRET a confidence interval for the slope β of the population regression line</li> </ul>			
			• REDECIPIN a similar part of short the short \$ of a modulus a			
			<ul> <li>FEREORIA a significance test about the slope p-of a population regression line</li> </ul>			
			INTERPRET computer output from a least-souares regression analysis			

#### Summarize, represent, and interpret data on a single count or measurement variable

CCSS.Math.Content.HSS-ID.A.1 Represent data with plots on the real number line (dot plots, histograms, and box plots).

CCSS.Math.Content.HSS-ID.A.2 Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.

CCSS.Math.Content.HSS-ID.A.3 Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).

CCSS.Math.Content.HSS-ID.A.4 Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use calculators, spreadsheets, and tables to estimate areas under the normal curve.

Summarize, represent, and interpret data on two categorical and quantitative variables

CCSS.Math.Content.HSS-ID.B.5 Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.

CCSS.Math.Content.HSS-ID.B.6 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.

CCSS.Math.Content.HSS-ID.B.6a Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, guadratic, and exponential models.

CCSS.Math.Content.HSS-ID.B.6b Informally assess the fit of a function by plotting and analyzing residuals.

CCSS.Math.Content.HSS-ID.B.6c Fit a linear function for a scatter plot that suggests a linear association.

Interpret linear models

CCSS.Math.Content.HSS-ID.C.7 Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data. CCSS.Math.Content.HSS-ID.C.8 Compute (using technology) and interpret the correlation coefficient of a linear fit. CCSS.Math.Content.HSS-ID.C.9 Distinguish between correlation and causation.

### Understand and evaluate random processes underlying statistical experiments

CCSS.Math.Content.HSS-IC.A.1 Understand statistics as a process for making inferences about population parameters based on a random sample from that population. CCSS.Math.Content.HSS-IC.A.2 Decide if a specified model is consistent with results from a given data-generating process, e.g., using simulation. For example, a model says a spinning coin falls heads up with probability 0.5. Would a result of 5 tails in a row cause you to question the model? Make inferences and justify conclusions from sample surveys, experiments, and observational studies

CCSS.Math.Content.HSS-IC.B.3 Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each. CCSS.Math.Content.HSS-IC.B.4 Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling. CCSS.Math.Content.HSS-IC.B.5 Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant. CCSS.Math.Content.HSS-IC.B.6 Evaluate reports based on data.

### Understand independence and conditional probability and use them to interpret data

CCSS.Math.Content.HSS-CP.A.1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not").

CCSS.Math.Content.HSS-CP.A.2 Understand that two events A and B are independent if the probability of A and B occurring together is the product of their probabilities, and use this characterization to determine if they are independent.

CCSS.Math.Content.HSS-CP.A.3 Understand the conditional probability of A given B as P(A and B)/P(B), and interpret independence of A and B as saying that the conditional probability of A given B is the same as the probability of A, and the conditional probability of B given A is the same as the probability of B.

CCSS.Math.Content.HSS-CP.A.4 Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. For example, collect data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results. CCSS.Math.Content.HSS-CP.A.5 Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. For example, compare the chance of having lung cancer.

Use the rules of probability to compute probabilities of compound events.

CCSS.Math.Content.HSS-CP.B.6 Find the conditional probability of A given B as the fraction of B's outcomes that also belong to A, and interpret the answer in terms of the model.

CCSS.Math.Content.HSS-CP.B.7 Apply the Addition Rule, P(A or B) = P(A) + P(B) - P(A and B), and interpret the answer in terms of the model.

CCSS.Math.Content.HSS-CP.B.8 (+) Apply the general Multiplication Rule in a uniform probability model, P(A and B) = P(A)P(B|A) = P(B)P(A|B), and interpret the answer in terms of the model. CCSS.Math.Content.HSS-CP.B.9 (+) Use permutations and combinations to compute probabilities of compound events and solve problems.

#### Calculate expected values and use them to solve problems

CCSS.Math.Content.HSS-MD.A.1 (+) Define a random variable for a quantity of interest by assigning a numerical value to each event in a sample space; graph the corresponding probability distribution using the same graphical displays as for data distributions.

CCSS.Math.Content.HSS-MD.A.2 (+) Calculate the expected value of a random variable; interpret it as the mean of the probability distribution.

CCSS.Math.Content.HSS-MD.A.3 (+) Develop a probability distribution for a random variable defined for a sample space in which theoretical probabilities can be calculated; find the expected value. For example, find the theoretical probability distribution for the number of correct answers obtained by guessing on all five questions of a multiple-choice test where each question has four choices, and find the expected grade under various grading schemes.

CCSS.Math.Content.HSS-MD.A.4 (+) Develop a probability distribution for a random variable defined for a sample space in which probabilities are assigned empirically; find the expected value. For example, find a current data distribution on the number of TV sets per household in the United States, and calculate the expected number of sets per household. How many TV sets would you expect to find in 100 randomly selected households?

Use probability to evaluate outcomes of decisions

CCSS.Math.Content.HSS-MD.B.5 (+) Weigh the possible outcomes of a decision by assigning probabilities to payoff values and finding expected values.

CCSS.Math.Content.HSS-MD.B.5a Find the expected payoff for a game of chance. For example, find the expected winnings from a state lottery ticket or a game at a fast-food restaurant.

CCSS.Math.Content.HSS-MD.B.5b Evaluate and compare strategies on the basis of expected values. For example, compare a high-deductible versus a low-deductible automobile insurance policy using various, but reasonable, chances of having a minor or a major accident.

CCSS.Math.Content.HSS-MD.B.6 (+) Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator).

CCSS.Math.Content.HSS-MD.B.7 (+) Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game).